

Name:

Date:

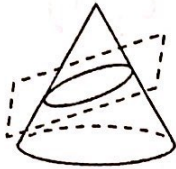
Topic:

Class:

Main Ideas/Questions

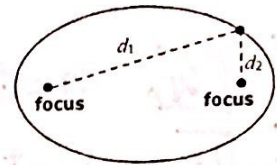
Notes/Examples

ELLIPSES



An ellipse is a set of points such that the **sum** of the distances from any point on the ellipse to two fixed points remains constant. These fixed points are called the **foci** of the ellipse.

$d_1 + d_2$ remains constant for all points on the ellipse!



MORE PARTS

Major Axis: The longer axis of symmetry.

Minor Axis: The shorter axis of symmetry.

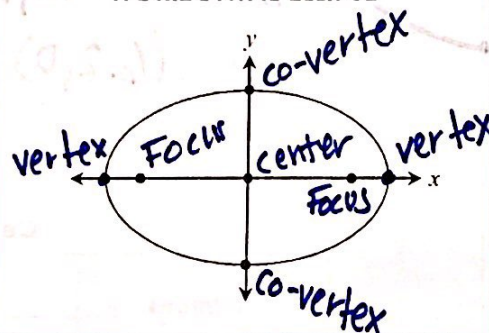
Center: The point at which the major and minor axis intersect.

Vertices: The endpoints of the major axis.

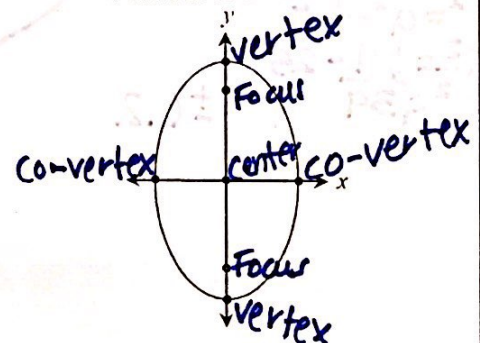
Co-Vertices: The endpoints of the minor axis.

TYPES OF ELLIPSES

HORIZONTAL ELLIPSE



VERTICAL ELLIPSE



- The vertices are $\pm a$ units away from the center.
 - The co-vertices are $\pm b$ units away from the center.
 - Length of Major Axis: $2a$; Length of Minor Axis: $2b$
 - The foci are $\pm c$ units away from the center.
 - Formula to find c : $c^2 = a^2 - b^2$
- $a > b$

STANDARD FORM

Center at $(0, 0)$

$$\frac{x^2}{a^2} + \frac{y^2}{b^2} = 1 \quad (\text{Hor.})$$

$$\frac{x^2}{b^2} + \frac{y^2}{a^2} = 1 \quad (\text{vert.})$$

STANDARD FORM

Center at (h, k)

$$\frac{(x-h)^2}{a^2} + \frac{(y-k)^2}{b^2} = 1$$

$$\frac{(x-h)^2}{b^2} + \frac{(y-k)^2}{a^2} = 1$$

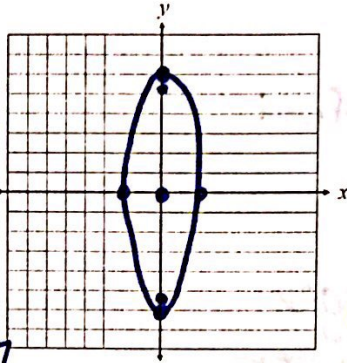
GRAPHING ELLIPSES

- ✓ Write the equation in **standard form**.
- ✓ Graph the **center**, (h, k) .
- ✓ Graph the **vertices**, using the larger denominator, a .
- ✓ Graph the **co-vertices**, using the smaller denominator, b .
- ✓ Use the formula $c^2 = a^2 - b^2$ to find and graph the **foci**.

Directions: Graph each ellipse. Identify the center, vertices, co-vertices, and foci.

1. $\frac{x^2}{4} + \frac{y^2}{36} = 1$

$\sqrt{a^2} = \sqrt{36} \quad a = \pm 6$
 $\sqrt{b^2} = \sqrt{4} \quad b = \pm 2$
 $c^2 = a^2 - b^2$
 $\sqrt{c^2} = \sqrt{36 - 4}$
 $c = \pm 5.7$



Center: $(0, 0)$

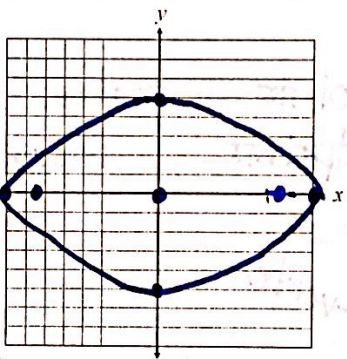
a Vertices: $(0, \pm 6)$

b Co-Vertices: $(\pm 2, 0)$

c Foci: $(0, \pm 5.7)$

2. $\frac{x^2}{64} + \frac{y^2}{25} = 1$

$\sqrt{a^2} = \sqrt{64} \quad a = \pm 8$
 $\sqrt{b^2} = \sqrt{25} \quad b = \pm 5$
 $c^2 = a^2 - b^2$
 $\sqrt{c^2} = \sqrt{64 - 25}$
 $c = \pm 6.2$



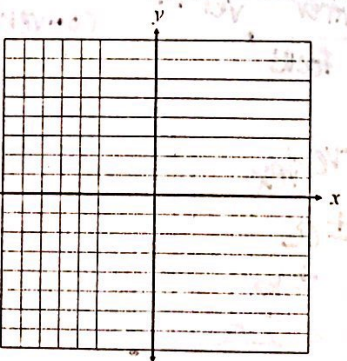
Center: $(0, 0)$

a Vertices: $(8, 0) (-8, 0)$

b Co-Vertices: $(0, 5) (0, -5)$

c Foci: $(6.2, 0) (-6.2, 0)$

3. $\frac{(x+1)^2}{49} + \frac{(y-2)^2}{9} = 1$



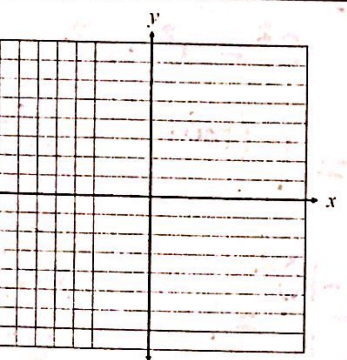
Center: _____

Vertices: _____

Co-Vertices: _____

Foci: _____

4. $\frac{(x-3)^2}{25} + \frac{(y-1)^2}{4} = 1$



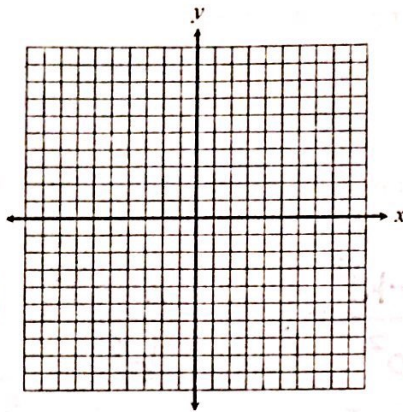
Center: _____

Vertices: _____

Co-Vertices: _____

Foci: _____

$$5. \frac{(x+4)^2}{20} + \frac{(y+2)^2}{36} = 1$$



Center: _____

Vertices: _____

Co-Vertices: _____

Foci: _____

$$6. \frac{9x^2}{144} + \frac{16y^2}{144} = \frac{144}{144}$$

$$\frac{x^2}{16} + \frac{y^2}{9} = 1$$

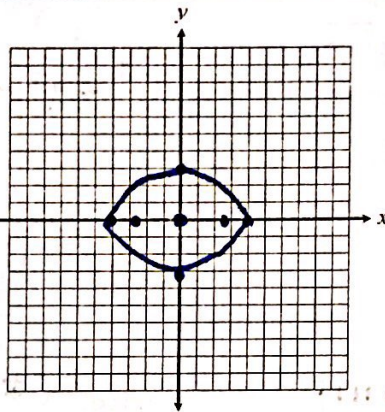
$$a^2 = 16 \quad a = \pm 4$$

$$b^2 = 9 \quad b = \pm 3$$

$$c^2 = 16 - 9$$

$$c^2 = 7$$

$$c = \pm 2.7$$



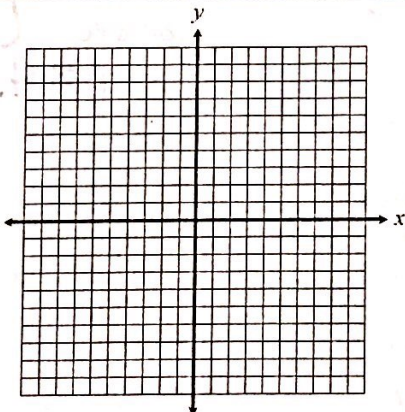
Center: (0,0)

Vertices: (±4,0)

Co-Vertices: (0, ±3)

Foci: (±2.7, 0)

$$7. x^2 + 4y^2 - 10x = -9$$



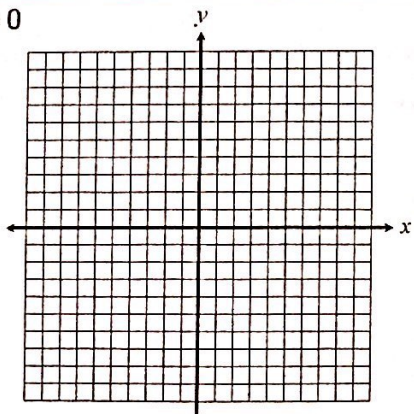
Center: _____

Vertices: _____

Co-Vertices: _____

Foci: _____

$$8. 4x^2 + y^2 - 32x + 8y + 76 = 0$$



Center: _____

Vertices: _____

Co-Vertices: _____

Foci: _____

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Main Ideas/Questions Notes/Examples

Writing Equations of ELLIPSES

Standard Form for the Equation of an Ellipse at Center (h, k):

HORIZONTAL ELLIPSE
(x-h)^2/a^2 + (y-k)^2/b^2 = 1

VERTICAL ELLIPSE:
(x-h)^2/b^2 + (y-k)^2/a^2 = 1

- a is the distance from the center to the vertices; (MAJOR AXIS)
b is the distance from the center to the co-vertices; (MINOR AXIS)
To find the foci use the formula, c^2 = a^2 - b^2 a > b

SET I:
Given a Graph
c^2 = a^2 - b^2
c^2 = (6)^2 - (4)^2
c^2 = sqrt(20)
c = +/- 4.5

Directions: Write an equation for each ellipse. Identify the center, vertices, co-vertices, and foci.

1. [Graph of a horizontal ellipse centered at (0,0) with vertices at (6,0) and (-6,0), and co-vertices at (0,4) and (0,-4).]

Equation: y = x^2/36 + y^2/16
Center: (0,0)
Vertices: (+/- 6, 0)
Co-Vertices: (0, +/- 4)
Foci: (+/- 4.5, 0)

2. [Graph of a vertical ellipse centered at (0,0) with vertices at (0,4) and (0,-4), and co-vertices at (3,0) and (-3,0).]

Equation: _____
Center: _____
Vertices: _____
Co-Vertices: _____
Foci: _____

3. [Graph of a horizontal ellipse centered at (2, -1) with vertices at (4, -1) and (0, -1), and co-vertices at (2, 0) and (2, -2).]

Equation: _____
Center: _____
Vertices: _____
Co-Vertices: _____
Foci: _____

SET 2:

Given Vertices,
Co-Vertices, & Foci

- ✓ Find the **center** (h, k) . (Use the midpoint formula with the vert. or co-vert.)
- ✓ Use the **vertices** to find a ; Use the **co-vertices** to find b .
*If given the foci, use the formula $c^2 = a^2 - b^2$ to find the missing part.
- ✓ Determine the direction of the ellipse to write the equation.

Directions: Write an equation for each ellipse with the given information.

4. Vertices: $(-5, 0)$ and $(5, 0)$
Co-Vertices: $(0, -2)$ and $(0, 2)$

$$C: (0, 0)$$

$$a = \pm 5 \quad a^2 = 25 \text{ (x)}$$

$$b = \pm 2 \quad b^2 = 4 \text{ (y)}$$

$$\boxed{\frac{x^2}{25} + \frac{y^2}{4} = 1}$$

5. Vertices: $(0, -8)$ and $(0, 8)$
Co-Vertices: $(-6, 0)$ and $(6, 0)$

$$C: (0, 0)$$

$$a = \pm 8 \quad a^2 = 64 \text{ (y)}$$

$$b = \pm 6 \quad b^2 = 36 \text{ (x)}$$

$$\boxed{\frac{x^2}{36} + \frac{y^2}{64} = 1}$$

6. Vertices: $(-5, 1)$ and $(1, 1)$
Co-Vertices: $(-2, 3)$ and $(-2, -1)$

7. Vertices: $(5, 8)$ and $(5, -6)$
Co-Vertices: $(11, 1)$ and $(-1, 1)$

8. Vertices: $(0, 6)$ and $(-10, 6)$
Foci: $(-2, 6)$ and $(-8, 6)$

9. Vertices: $(-9, -2)$ and $(-9, -12)$
Foci: $(-9, -3)$ and $(-9, -11)$

10. Co-Vertices: $(5, 0)$ and $(-5, 0)$
Foci: $(0, 12)$ and $(0, -12)$

11. Co-Vertices: $(2, 7)$ and $(2, -9)$
Foci: $(-4, -1)$ and $(8, -1)$

$$C: (0, 0)$$

$$b = \pm 5 \quad b^2 = 25 \text{ (x)}$$

$$c = \pm 12 \quad c^2 = 144$$

$$c^2 = a^2 - b^2$$

$$144 = a^2 - 25$$

$$169 = a^2 \text{ (y)}$$

$$\boxed{\frac{x^2}{25} + \frac{y^2}{169} = 1}$$