

* REMEMBER $\sqrt{-1} = i$ *

Factor Completely.

1) $\frac{2x^2 + 66x + 120}{2} = 2(x^2 + 33x + 60)$

2) $\frac{9x^2 + 75}{3} = 3(3x^2 + 25)$

3) $\frac{2x^4y^2 - 4x^3y^3 + 8xy^4 - 12x^4y^5}{2xy^2} = 2xy^2(x^3 - 2x^2y + 4y^2 - 6x^3y^3)$

4) $(x+4)^2 - 81$
 $(x+4+9)(x+4-9)$
 $(x+13)(x-5)$

Solve.

5) $16x^2 = 25$
 $\sqrt{x^2} = \sqrt{\frac{25}{16}}$
 $x = \pm \frac{5}{4}$

6) $x^2 + 6x + 8 = 0$
 $(x+4)(x+2) = 0$
 $x+4=0 \quad x+2=0$
 $x=-4 \quad x=-2$

7) $3x^2 = -12$
 $\sqrt{x^2} = \sqrt{-4}$
 $x = \pm 2i$

8) $9x^2 - 54 = 0$
 $9x^2 = 54$
 $\sqrt{x^2} = \sqrt{6}$
 $x = \pm \sqrt{6}$

9) $2x^2 + 36 = 0$
 $2x^2 = -36$
 $\sqrt{x^2} = \sqrt{-18}$
 $x = \pm 3i\sqrt{2}$

10) $x^2 - 10 = 0$
 $\sqrt{x^2} = \sqrt{10}$
 $x = \pm \sqrt{10}$

11) $x^2 - 9x + 18 = 0$
 $(x-6)(x-3) = 0$
 $x-6=0 \quad x-3=0$
 $x=6 \quad x=3$

12) $2x^2 - 3 = 0$
 $2x^2 - x - 3 = 0$
 $(2x+3)(x-1) = 0$
 $2x+3=0 \quad x-1=0$
 $x = -\frac{3}{2} \quad x=1$

13) $3x^2 + 12x = 0$
 $3x(x+4) = 0$
 $3x=0 \quad x+4=0$
 $x=0 \quad x=-4$

14) $3x^2 - 16x - 12 = 0$
 $(x-18)(x+2) = 0$
 $(x-6)(3x+2) = 0$
 $x-6=0 \quad 3x+2=0$
 $x=6 \quad 3x=-2$
 $x = -\frac{2}{3}$

15) $x^2 - 5x = 0$
 $x(x-5) = 0$
 $x=0 \quad x-5=0$
 $x=5$

16) $9x^2 - 16 = 0$
 $9x^2 = 16$
 $\sqrt{x^2} = \sqrt{\frac{16}{9}}$
 $x = \pm \frac{4}{3}$

17) $25x^2 - 15x = 0$
 $5x(5x-3) = 0$

$\frac{5x}{5} = \frac{0}{5}$

$X = 0$

$\frac{5x-3}{+3 +3} = 0$

$\frac{5x}{5} = \frac{3}{5}$
 $X = \frac{3}{5}$

18) $4x^2 + 8 = 0$
 $\frac{-8}{-8} -8$
 $\frac{4x^2}{4} = \frac{-8}{4}$
 $\sqrt{x^2} = \sqrt{-2}$
 $X = \pm i\sqrt{2}$

19) $x^2 + 8x = -16$
 $\frac{+16}{+16} +16$
 $X^2 + 8x + 16 = 0$
 $(x+4)(x+4) = 0$
 $X = -4, -4$

~~$\frac{16}{8}$~~
 ~~$\frac{4}{4}$~~

Slip & Divide
 ~~$\frac{-18}{-18}$~~
 ~~$\frac{9}{7}$~~

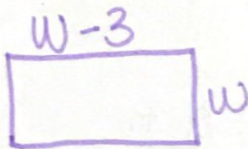
22) $6x^2 + 7x - 3 = 0$
 $(x+\frac{3}{2})(x-\frac{1}{3}) = 0$
 $(2x+3)(3x-1) = 0$
 $\frac{2x+3}{-3 -3} = 0$
 $\frac{3x-1}{+1 +1} = 0$
 $\frac{2x}{2} = \frac{-3}{2}$
 $\frac{3x}{3} = \frac{1}{3}$
 $X = -\frac{3}{2}$
 $X = \frac{1}{3}$

Grouping
 ~~$\frac{6}{-6}$~~
 ~~$\frac{-1}{-7}$~~

20) $3x^2 - 7x + 2 = 0$
 $(\frac{3x^2}{3x} - \frac{6x}{3x}) - (\frac{x+2}{-1 -1}) = 0$
 $3x(x-2) - 1(x-2) = 0$
 $(x-2)(3x-1) = 0$
 $X-2 = 0$
 $X = 2$
 $\frac{3x-1}{+1 +1} = 0$
 $\frac{3x}{3} = \frac{1}{3}$
 $X = \frac{1}{3}$

21) $5x^2 - 80 = 0$
 $\frac{+80}{+80} +80$
 $\frac{5x^2}{5} = \frac{80}{5}$
 $\sqrt{x^2} = \sqrt{16}$
 $X = \pm 4$

23) The length of a rectangle is 3ft less than the width. The area is 40ft². What is the width and the length of the rectangle?

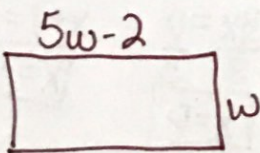


$A = lw$
 $40 = (w-3)w$
 $40 = w^2 - 3w$
 $\frac{-40}{-40}$
 $0 = w^2 - 3w - 40$
 $0 = (w-8)(w+5)$

$\frac{w-8}{+8 +8} = 0$
 $\frac{w+5}{-5 -5} = 0$
 $w = 8$
 ~~$w = -5$~~
Width 8ft
Length 5ft

~~$\frac{-40}{-8}$~~
 ~~$\frac{5}{-3}$~~

24) The length of a picture is two less than five times the width. If the area is 39 cm², what is the length and width of the picture?



$A = lw$
 $39 = (5w-2)w$
 $39 = 5w^2 - 2w$
 $\frac{-39}{-39}$
 $0 = 5w^2 - 2w - 39$
 $0 = (5w^2 - 15w) + (13w - 39)$
 $0 = 5w(w-3) + 13(w-3)$
 $0 = (w-3)(5w+13)$

$\frac{w-3}{+3 +3} = 0$
 $\frac{5w+13}{-13 -13} = 0$
 $w = 3$
 ~~$w = -\frac{13}{5}$~~

~~$\frac{-195}{-15}$~~
 ~~$\frac{13}{-2}$~~

Grouping

Width 3cm
Length 13cm