

Writing in Sigma Notation and Finding Terms

nth Partial Sum: the sum of the first n terms of a series.

1) Find the 4th partial sum of $a_n = (-2)^n + 3$

$$1 + 7 + (-5) + 19 =$$

$$\boxed{22}$$

2) Find S_3 of $a_n = \frac{4}{10^n}$

$$0.4 + 0.04 + 0.004 \\ = \boxed{0.444}$$

3) Write the series in sigma notation. The lower bound is given.

$-2 - 1 + 0 + 1 + 2 + 3 + 4 + 5 ; n = 1$ $d = 1$

$$\sum_{n=1}^8 (n-3)$$

$$a_n = a_1 + (n-1)d$$

$$a_n = -2 + (n-1)(1)$$

$$a_n = -2 + n - 1$$

$$a_n = n - 3$$

4) Write the arithmetic series in sigma notation. The lower bound is given.

$a_1 = -\frac{14}{5}$, $a_2 = -\frac{13}{5}$, $d = -\frac{1}{5}$, $n = 2$

$$-\frac{14}{5} + \left(-\frac{13}{5}\right) + \left(-\frac{12}{5}\right) + \left(-\frac{11}{5}\right) + \dots + \left(-\frac{3}{5}\right); n = 2$$

$$d = -\frac{11}{5} - \left(-\frac{12}{5}\right) = \frac{1}{5}$$

$$\sum_{n=2}^{12} \left(\frac{1}{5}n - 3\right)$$

$$a_n = a_1 + (n-1)d$$

$$a_n = -\frac{14}{5} + (n-1)\left(\frac{1}{5}\right)$$

$$a_n = -\frac{14}{5} + \frac{1}{5}n - \frac{1}{5}$$

$$a_n = \frac{1}{5}n - \frac{15}{5}$$

5) Write each geometric series in sigma notation.

$a_1 = 0.2$, $r = 5 \div (-1) = -5$

$$\sum_{n=1}^6 0.2(-5)^{n-1}$$

$$a_n = a_1 r^{n-1}$$

$$a_n = 0.2(-5)^{n-1}$$

(P.595: 29-35 odd, 58-62; P.605: 63-68; P.616: 97-100)