

$$\textcircled{1} a^2 = 23^2 + 13^2 - 2(23)(12)\cos 120$$

$$\sqrt{a^2} = \sqrt{997}$$

$$\boxed{a = 31.6}$$

$$23^2 = 31.6^2 + 13^2 - 2(31.6)(13)\cos C$$

$$529 = 1167.56 - 821.6 \cos C$$

$$-638.56 = -821.6 \cos C$$

$$0.7772 = \cos C$$

$$\boxed{\cos^{-1} C = 39.0^\circ}$$

$$\angle B = 180 - 39.0 - 120 = \boxed{21^\circ}$$

$$\textcircled{3} c = 26, b = 24, a = 18$$

$$26^2 = 24^2 + 18^2 - 2(24)(18)\cos C$$

$$676 = 900 - 864 \cos C$$

$$-224 = -864 \cos C$$

$$0.2593 = \cos C$$

$$\boxed{\cos^{-1} C = 75.0^\circ}$$

$$24^2 = 26^2 + 18^2 - 2(26)(18)\cos B$$

$$576 = 1000 - 936 \cos B$$

$$-424 = -936 \cos B$$

$$0.4530 = \cos B$$

$$\boxed{\cos^{-1} B = 63.1^\circ}$$

$$\angle A = 180 - 63.1 - 75.0 = \boxed{41.9^\circ}$$

$$\textcircled{2} 23^2 = 21^2 + 17^2 - 2(21)(17)\cos B$$

$$529 = 730 - 714 \cos B$$

$$-201 = -714 \cos B$$

$$0.2815 = \cos B$$

$$\boxed{\cos^{-1} B = 73.6^\circ}$$

$$21^2 = 23^2 + 17^2 - 2(23)(17)\cos A$$

$$441 = 818 - 782 \cos A$$

$$-377 = -782 \cos A$$

$$0.4821 = \cos A$$

$$\boxed{\cos^{-1} A = 61.2^\circ}$$

$$\angle C = 180 - 61.2 - 73.6 = \boxed{45.2^\circ}$$

$$\textcircled{4} b = 21, a = 18, m\angle C = 116^\circ$$

$$c^2 = 21^2 + 18^2 - 2(21)(18)\cos 116$$

$$\sqrt{c^2} = \sqrt{1096.41}$$

$$\boxed{c = 33.1}$$

$$21^2 = 33.1^2 + 18^2 - 2(33.1)(18)\cos B$$

$$441 = 1419.61 - 1191.6 \cos B$$

$$-978.61 = -1191.6 \cos B$$

$$0.8213 = \cos B$$

$$\boxed{\cos^{-1} B = 34.8^\circ}$$

$$\angle A = 180 - 34.8 - 116 = \boxed{29.2^\circ}$$

$$\textcircled{5} b = 8.8, a = 13.5, c = 18.5$$

$$18.5^2 = 8.8^2 + 13.5^2 - 2(8.8)(13.5)\cos C$$

$$342.25 = 259.69 - 237.6\cos C$$

$$82.56 = -237.6\cos C$$

$$-0.3475 = \cos C$$

$$\boxed{\cos^{-1} C = 110.3^\circ}$$

$$13.5^2 = 8.8^2 + 18.5^2 - 2(8.8)(18.5)\cos A$$

$$182.25 = 419.69 - 325.6\cos A$$

$$-237.44 = -325.6\cos A$$

$$0.7292 = \cos A$$

$$\boxed{\cos^{-1} A = 43.2^\circ}$$

$$\angle B = 180 - 110.3 - 43.2 = \boxed{26.5^\circ}$$

$$\textcircled{7} A = \frac{1}{2}(13)(14)\sin 74$$

$$\boxed{A = 87.5 \text{ km}^2}$$

$$\textcircled{9} \angle D = 180 - 44 - 18 = 118$$

$$\frac{\sin 118}{14} = \frac{\sin 18}{c}$$

$$c \frac{\sin 118}{\sin 118} = \frac{14 \sin 18}{\sin 118}$$

$$c = 4.9$$

$$A = \frac{1}{2}(4.9)(14)\sin 44$$

$$\boxed{A = 23.8 \text{ cm}^2}$$

$$\textcircled{6} a = 11, c = 22, m\angle B = 46^\circ$$

$$b^2 = 11^2 + 22^2 - 2(11)(22)\cos 46$$

$$\sqrt{b^2} = \sqrt{268.785}$$

$$\boxed{b = 16.4}$$

$$22^2 = 11^2 + 16.4^2 - 2(11)(16.4)\cos C$$

$$484 = 389.96 - 360.8\cos C$$

$$94.04 = -360.8\cos C$$

$$-0.2606 = \cos C$$

$$\boxed{\cos^{-1} C = 105.1^\circ}$$

$$\angle A = 180 - 105.1 - 46 = \boxed{28.9^\circ}$$

$$\textcircled{8} \angle Z = 180 - 35 - 126 = 19^\circ$$

$$\frac{\sin 19}{z} = \frac{\sin 126}{12.7}$$

$$\frac{12.7 \sin 19}{\sin 126} = \frac{z \sin 126}{\sin 126}$$

$$5.1 = z$$

$$A = \frac{1}{2}(5.1)(12.7)\sin 35$$

$$\boxed{A = 18.6 \text{ in}^2}$$

$$\textcircled{10} \frac{\sin 40}{11} = \frac{\sin B}{6.4}$$

$$\frac{6.4 \sin 40}{11} = \frac{11 \sin B}{11}$$

$$0.374 = \sin B$$

$$\sin^{-1} B = 22.0^\circ$$

$$\angle A = 180 - 22.0 - 40 = 118$$

$$A = \frac{1}{2}(11)(6.4)\sin 118$$

$$\boxed{A = 31.1 \text{ in}^2}$$

$$\textcircled{11} \quad S = \frac{7 + 14 + 15}{2}$$

$$S = 18$$

$$A = \sqrt{18(18-7)(18-14)(18-15)}$$

$$A = 48.7 \text{ in}^2$$

$$\textcircled{12} \quad S = \frac{5 + 11 + 13}{2}$$

$$S = 14.5$$

$$A = \sqrt{14.5(14.5-5)(14.5-11)(14.5-13)}$$

$$A = 26.9 \text{ yd}^2$$